Adding a piece wise linear noise source to a free running oscillator can show how the noise maps to jitter or PM or to a spectrum.

In this case a 2 second/1kHz BW random PWL file is created.
But in this case, a jitter plot will be taken and used to produce a PWL file, which then can be used to Phase Modulate a 20 Hz signal.


Noise from BPWL is applied to one of the inputs of the amplifier BAMP. Amplifier BAMP is clipping its output at +/- 10Volts.

Capacitor C1 is toggling between +/- 5volts. Noise source BPWL is messing up the timing. So in this case $C 1$ has been adjusted to produce 40 whole cycles within 2 seconds.

Noise source BPWL is receiving a random 1VRMS signal with a bandwidth of 1 KHz . This has been scaled down to +/- 100mV rms.


The Noise source BPWL can be seen on the inp input. But its PM effects are hard to see. A jitter plot can show better details.

| compose | anysize | start $=0$ stop $=99$ step $=1$ |
| :---: | :---: | :---: |
| let | num $=$ | length(out2)-5 |
| let i = | 0 |  |
| let $\mathrm{t}=$ | 0 |  |
| let $\mathrm{n}=$ | 0 |  |

Assume the number of rising or falling edges are not known at this point. So array anysize will be used to store an unknown number of data points. The total number of output points (num) for the oscillator output is easy to find.

Some simple "if" statements can be used to find the timing for the edges.

```
\begin{tabular}{|c|c|}
\hline repeat & \$\&num \\
\hline if & ( out2[i] < 0 \& out2[i+1] > 0) \\
\hline let \(\mathrm{t}=\) & time[i] \\
\hline let & anysize[n]= t \\
\hline echo & \(\mathrm{n}=\) \$ \(\mathrm{S}^{\text {n }}\) out_rise= \$\&t \\
\hline let endif & \(\mathrm{n}=\mathrm{n}+1\) \\
\hline if & ( out2[i] > 0 \& out2[i+1] < 0) \\
\hline let \(\mathrm{t}=\) & time[i] \\
\hline let & anysize[n] \(=t\) \\
\hline echo & \(\mathrm{n}=\quad \$ \& \mathrm{n}\) out_fall= \$\&t \\
\hline let endif & \(\mathrm{n}=\mathrm{n}+1\) \\
\hline let \(\mathrm{i}=\) endrepeat & i +1 \\
\hline let & \(\mathrm{n} 3=\mathrm{n}-1\) \\
\hline
\end{tabular}
```


## The MacSpice printout..

| $\mathrm{n}=0$ | out_rise $=0.0159425$ |
| :--- | :--- |
| $\mathrm{n}=1$ | out_fall $=0.0402975$ |
| $\mathrm{n}=2$ | out_rise $=0.0642775$ |
| $\mathrm{n}=3$ | out_fall $=0.0891075$ |
| $\mathrm{n}=4$ | out_rise $=0.114012$ |
| $\mathrm{n}=5$ | out_fall $=0.138993$ |
| $\mathrm{n}=6$ | out_rise $=0.164068$ |
| $\cdots$ |  |
| $\mathrm{n}=76$ | out_rise $=1.91342$ |
| $\mathrm{n}=77$ out_fall $=1.9383$ |  |
| $\mathrm{n}=78$ out_rise $=1.96327$ |  |
| $\mathrm{n}=79$ out_fall $=1.98833$ |  |

Now that the number of edge data points are known, some new arrays can be created to store and plot
the results.



In this case rtp stands for time reference point. That is the time when the transition happened. The value tp stands for time period. This is the actual time between edges. Notice that the average time period is 25 msec . A 20 Hz square wave has two transitions within 50 msec .

It is easy to do some further math on the data.

| let | tpave $\overline{=}$ mean ( $t \overline{\mathrm{p}}$ ) |
| :---: | :---: |
| let | tpac $=$ tp -tpave |
| plot | tpac vs rtp |
|  | Find_RMS_Vtpac========================= |
| let | i $=0$ |
| let | vpwr $=0$ |
| repeat | \$\&n2 |
| let | $i=\quad i+1$ |
| let end | vpwr $=$ vpwr + (mag(tpac[i])*mag(tpac[i]))/n2 |
| let | vrms1 = sqrt(vpwr) |
| echo | Edge2Edge_Period \$\&tpave TPAC RMS SQUARE = \$\&vrms1 |



In this case tpac stands for time reference point AC. The average time period has been stripped away.

Now it is easy to do a RMS of the data and print out both the average and RMS levels.

The MacSpice printout...
Edge2Edge_Period 0.024968 TPAC RMS SQUARE $=0.000404478$
Consider the ratio of the RMS value to the Average value.

$$
\text { TimePeriod_RMS/AVE }=0.0162
$$



Capacitor C 1 is swinging between -5 V and +5 V .
And at each end there is an uncertainty of $+/-100 \mathrm{mV}$ rms. So in this case, the ratio of the RMS value to Average value is.

```
C1_TimePeriod_RMS/AVE = sqrt(2)*100mv/10v = 0.01414
```

The two ratios of uncertainty to average value should come close to each other. The amplifier BAMP is in effect sampling two 100 mV rms random points to be compared to a l0volt swing. That ratio of uncertainty to the average value gets directly mapped to the time period uncertainty.

Now this 100 mV rms noise has a 1 kHz bandwidth. Even though a grand total of 80 samples of this noise is taken over 2 seconds, the RMS value for all samples is still 100mV. This is a case
of sampling without an anti-aliasing filter. So the 1 kHz noise just got all alaised down to within a 20 Hz bandwidth.

But variation in time period is really frequency modulation. All the ac time periods need to be added up to see the overall phase timing.

```
*==========Convert_FM_to_PM=================================================
let i = 1
let n2 = n -1
repeat $&n2
let td[i] = td[i-1] +tpac[i]
let i = i +1
endrepeat
plot td vs rtp
```



```
let tdave = mean(t\overline{d})
let tdac = td -tdave
plot tdac vs rtp
```


$\mathrm{ms} \quad$ - tdac


In this case tdac stands for time delay AC. This is how much each edge is "delayed" in time compared to a perfect 20 Hz square wave.

This can further be converted to a phase modulation format in terms of radians.

```
*=========Convert to PM radian===============================================
let pmr =3.\overline{1415}9*\overline{tdac/tpave}
plot pmr vs rtp
```

munits pmr


Now pmr stands for phase modulation radians. In this format, the jitter can be treated like a modulation signal which can be exported to a piece wise linear file.


## The PWL FileJitter.inc file comes out looking like so.

| VpwlT OUT O PWL ( |  |
| :--- | :--- |
| +0.0402975 | -0.298113 |
| +0.0642775 | -0.315477 |
| +0.0891075 | -0.3235 |
| +0.114012 | -0.321894 |
| +.0 .88921 | -0.107741 |
| +1.813132 | -0.119442 |
| +1.9383 | -0.118562 |
| +1.96327 | -0.107615 |
| +1.98833 | -0.0966681 |
| + |  |



* Vpwlt OUT $0 \quad$ PWL ( +0.00050 .988835 +.....

| .include | PWL_Fi | le.inc |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Rload | OUT | 0 | 1k |  |  |
| BAMP | OUT1 | 0 | $\mathrm{V}=$ | 9.9*tanh( | (V(INP) -V (INN) ) * 10 ) |
| RO | OUT1 | OUT2 | 1 |  |  |
| C0 | OUT2 | 0 | 500u |  |  |
| R1 | VFB | 0 | 1K |  |  |
| R2 | VFB | OUT2 | 1K |  |  |
| R3 | INN | OUT2 | 2.49K |  |  |
| BPWL | INP | VFB | $\mathrm{V}=$ | . 1 *V(OUT) |  |
| C1 | INN | 0 | 9.415u | IC= . 1 |  |
| *TRAN | TSTEP | TSTOP | TSTART | TMAX | ?UIC? |
| .tran <br> . control <br> run | 5 u | 2 | 0 | 5u | UIC |
| set | pensiz | $=$ | 2 |  |  |


let ph $=p m r[i]$
echo "+ \$\&t \$\&ph" >> \$outfile $i=i+1$
endrepeat
echo "+ )" >> \$outfile
*=========Wrap_Up============================================================1
.endc
.end
2.18.10_12.15PM
dsauersānjose@aol.com
Don Sauer
http://www.idea2ic.com/

